## Understanding the Structure of Large, Diverse Collections of Shapes

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**Princeton University** 

#### **3D repositories**



**Computer Graphics** 

**3D** Scanning

# Introduction **3D** repositories **Data Analysis** Paleonthology Molecular Biology **3**E **Computer Graphics** Pseudomonas aldolase









## **Previous Work**

Understanding structure

→ 3D shapes • Collections of 3D shapes



(c) Mitra et al., SIGGRAPH'06

(c) Golovinskiy et al. SIGGRAPH Asia'08

Symmetry

Segmentation

Saliency detection





(c) Lee et al. SIGGRAPH'05

## **Previous Work**

Understanding structure
3D shapes
Collections of 3D shapes



Light Standard Newspaper Box Car Traffic Light

(c) Golovinskiy et al., ICCV'09

Grouping



(c) Kalogerakis et al. SIGGRAPH'12

Part-based models

(c) Praun et al., SIGGRAPH'01

Correspondence

**Consistent Segmentation** 

(c) Golovinskiy et al., SMI'09













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#### Structure

Correspondences

Parts

Variations

Grouping

- 1. Blended Intrinsic Maps
- 2. Fuzzy Correspondences
- 3. Deformable Template

### **3D repositories**

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#### Structure

Correspondences

- Non-isometric shapes



Variations

Grouping

### **1. Blended Intrinsic Maps**

- 2. Fuzzy Correspondences
- 3. Deformable Template

**Complexity:** O(N<sup>2</sup>)

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#### Structure

Correspondences

- Non-isometric shapes
- Leverage power of the set



Variations

Grouping

#### 1. Blended Intrinsic Maps

#### 2. Fuzzy Correspondences

#### 3. Deformable Template

#### **Complexity:** O(N<sup>1.5</sup>)

### **3D repositories**

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#### Structure

Correspondences

- Non-isometric shapes
- Leverage power of the set

#### Parts

- Consistent for all shapes

#### Variations

- Extra and missing parts
- Deformations

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#### **3. Deformable Template**

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### **1. Blended Intrinsic Maps**

- 2. Fuzzy Correspondences
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#### Input

- A pair of manifold surfaces
- Related by a non-uniform (i.e. non-isometric) deformation



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#### Output

- A map defined at every point
- $\circ$  Smooth
- Low-distortion
- Aligns semantic features



## **Previous Work**

Pairwise Correspondence: Intrinsic

Gromov-Hausdorff

**OMÖbius Transformations** 



Bronstein et al., PNAS' 06

## **Previous Work**

#### Pairwise Correspondence: Intrinsic

- o Gromov-Hausdorff
- Möbius Transformations





#### Lipman and Funkhouser, SIGGRAPH'09

## **Our Approach**

Weighted combination of locally-isometric maps



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Weighted combination of locally-isometric maps



## **Our Approach**

Weighted combination of locally-isometric maps



## **The Computational Pipeline**



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Find consistent set of candidate maps



## **The Computational Pipeline**



## **Finding Blending Weights**

• For every point p • Compute a weight of each map m<sub>i</sub> at p



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• For every point p • Compute a weight of each map m<sub>i</sub> at p

We model the weight with deviation from isometry
 Area distortion for conformal maps




#### **The Computational Pipeline**



#### **Blending Maps**

Input for each point p:
An image m<sub>i</sub>(p) after applying each map m<sub>i</sub>
A blending weight for each map



### **Blending Maps**

Input for each point p:
An image m<sub>i</sub>(p) after applying each map m<sub>i</sub>
A blending weight for each map

Output for each point:
 Weighted geodesic centroid of { m<sub>i</sub>(p) }



#### Results



#### Failures



## Comparison



# Summary

Blend locally-isometric maps

- Robust to large non-uniform deformations
- Efficient to compute
- Outperforms other methods on benchmark

#### Goal

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#### **Complexity:** O(N<sup>1.5</sup>)

#### Goal

Find point correspondences for all pairs of models in collections with large geometric variations

- Diverse shapes
- Efficient computation



# **Previous Work**

#### Correspondences in a collection

- All pairwise alignments
- Template fitting
- Map optimization



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# Challenges

Efficient matching of diverse collections
Geometric alignment only works for similar shapes
Point-to-point correspondences do not handle ambiguity
Computing all pairwise alignments is O(N<sup>2</sup>)

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Diffusion map leverages transitivity:



Efficient matching of diverse collections

- Geometric alignment only works for similar shapes
- Point-to-point correspondences do not handle ambiguity
   Computing all pairwise alignments is O(N<sup>2</sup>)

Traditional correspondence:



Diffusion map produces continuous similarity values:



Efficient matching of diverse collections
Geometric alignment only works for similar shapes
Point-to-point correspondences do not handle ambiguity
Computing all pairwise alignments is O(N<sup>2</sup>)

Traditional correspondence:



Diffusion map works with sparse alignments







Chair 4















#### Pairwise Correspondences





#### Pairwise Correspondences

















Pairwise Correspondences









#### Larger embedding example

Embedding of 128 points from 7 planes



#### Larger embedding example

Embedding of 128 points from 7 planes


### Larger embedding example

Embedding of 128 points from 7 planes



### Larger embedding example

Embedding of 128 points from 7 planes



# **Computing Fuzzy Correspondences**

- 1. Sample points on each model
- 2. Select pairs of models to align
- 3. Estimate correspondences for selected pairs
- ↓ 4. Diffuse point correspondences
  - 5. Re-align pairs to improve consistency
    - Repeat until convergence













# Summary

### Fuzzy Correspondences via Diffusion

- Represent ambiguity in mapping
- Leverages transitivity to compare dissimilar shapes
- Far less than N<sup>2</sup> pairwise alignments are required

# **Talk Outline**

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#### Structure

### Correspondences

- Non-isometric shapes
- Semantic ambiguity
- Consistent for all pairs

#### Parts

- Consistent for all shapes

### Variations

- Extra and missing parts
- Deformations

#### Grouping

1. Blended Intrinsic Maps

### 2. Fuzzy Correspondences

### **3. Deformable Template**

#### **Complexity:** O(N)

## Goal

### **3D repositories**

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### Correspondences

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## **Previous Work**

### **3D repositories**



#### Structure

### Correspondences

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### Variations

- Extra and missing parts
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#### Grouping

#### Each paper focuses only on one aspect



(c) Kalogerakis et al., SIGGRPAPH'12



(c) Huang et al., SIGGRAPH Asia'12



(c) Sidi et al. SIGGRAPH Asia'11, Huang et al. SIGGRAPH Asia'11





(c) Hou et al., CAD'05

Learn part-based model with Gaussian distributions for

- Part positions
- Part anisotropic scales
- Part local shape features





Bench

**Dining chair** 

Swivel chair



InitialUnlabeled, unorganizedtemplate3D collection



Initial Unlabeled, unorganized template 3D collection

Final Deformable Templates



template 3D collection

Final Deformable Templates

Final Templates analysis results



Shape to template rigid alignment (r)

- Per part deformations (d)
  - Existence
  - Centroid position
  - Anisotropic scale
- Labeling of points in the shape (  $\ell$  )
- Shape  $\leftrightarrow$  template mapping (*m*)

## Method

**Template Initialization** 

- Template Fitting
  - **Template Refinement** 
    - repeat until convergence

## Method

- → Template Initialization
  - Template Fitting
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## **Template Initialization**

Manual initialization

- $\circ$  The user aligns boxes to semantic parts (  $\approx$  5 min)
- Automatic initialization
  - Automatically segment all shapes
  - Execute full template learning from best segmentations
  - Pick template with smallest average fitting energy

### Method

**Template Initialization** 

Template Fitting

**Template Refinement** 

repeat until convergence

# **Fitting Energy**

$$E = E_{\text{data}} + \gamma E_{\text{deform}} + \beta E_{\text{smooth}}$$

- $\circ E_{data}$  (template  $\leftrightarrow$  shape distance + local shape features)
- Edeform (plausibility of template deformation)
- Esmooth (close & similar regions should get the same label)



Alternate steps until shape segmentation converges:

- $\circ$  Segmentation (optimize  $\ell$ )
  - $\circ$  Correspondences (optimize m)
- $\,\circ\, {\sf Deformation}$  (optimize r,d )

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![](_page_97_Picture_5.jpeg)

Alternate steps until shape segmentation converges:

- Segmentation (optimize l)
  Correspondences (optimize m)
- $\,\circ\,$ Deformation (optimize r,d )

$$E = E_{\text{data}} + \gamma E_{\text{deform}} + \beta E_{\text{smooth}}$$

Method: Graph cut [Boykov et al. 2001]

![](_page_98_Picture_6.jpeg)

Alternate steps until shape segmentation converges:

- Segmentation (optimize  $\ell$ )
  - Correspondences (optimize m)
- $\,\circ\,$ Deformation (optimize r,d )

$$E = E_{\text{data}} + \gamma E_{\text{deform}} + \beta E_{\text{smooth}}$$

Method: Part-aware closest points

![](_page_99_Picture_7.jpeg)

Alternate steps until shape segmentation converges:

• • Segmentation (optimize  $\ell$ )

 $\circ$  Correspondences (optimize m)

- Deformation (optimize r, d )

$$E = E_{\text{data}} + \gamma E_{\text{deform}} + \beta E_{\text{smooth}}$$

Method: Solve for critical points.

position:  $\frac{\partial (E_{\text{data}} + E_{\text{deform}})}{\partial b_p} = 0$ scale:  $\frac{\partial (E_{\text{data}} + E_{\text{deform}})}{\partial b_s} = 0$ 

![](_page_100_Picture_8.jpeg)

## Method

**Template Initialization** 

- Template Fitting
- Template Refinement
  - repeat until convergence

Improve set of templates from unlabeled geometry

![](_page_102_Figure_2.jpeg)

**a.** Initial Template

Improve set of templates from unlabeled geometry

![](_page_103_Picture_2.jpeg)

**a.** Initial Template

**b.** Fitting Set

![](_page_104_Picture_2.jpeg)

![](_page_105_Figure_2.jpeg)

![](_page_106_Figure_2.jpeg)

![](_page_107_Figure_2.jpeg)
## Overview

Improve set of templates from unlabeled geometry



Update template set from deformations in Learning Set

- Update current
- $\circ \, \text{Spawn new}$
- Reject outliers



Current Template Set



#### Update template set from deformations in Learning Set



#### Update template set from deformations in Learning Set



#### Update template set from deformations in Learning Set

Update current



# Results

#### Evaluation

- Examples
- $\circ \, \textbf{Correspondence benchmark}$
- Segmentation benchmark
- Timing and complexity

## **3D Warehouse planes**



Randomly sampled template fitting results:





## **3D Warehouse bikes**





Final Templates:





Randomly sampled template fitting results:





# Results

#### Evaluation

- $\circ$  Examples
- Correspondence benchmark
   Segmentation benchmark
- Timing and complexity

## **Correspondences benchmark**



## **Correspondences benchmark**



# Results

#### Evaluation

- $\circ$  Examples
- Correspondence benchmark
- Segmentation benchmark
- Timing and complexity

## **Co-segmentation benchmark**



# Results

#### Evaluation

- $\circ$  Examples
- Correspondence benchmark
- Segmentation benchmark
- Timing and complexity

# **Timing and complexity**

Timing • 20 shapes: 2-3min • 100 shapes: 10-30 min • 3000 planes: 3.3 hrs • 7000 chairs: 10 hrs

# **Timing and complexity**

Timing

- o 20 shapes: 2-3min
- o 100 shapes: 10-30 min
- o 3000 planes: 3.3 hrs
- 07000 chairs: 10 hrs

#### Complexity

N - collection size, K<sub>L</sub> - learning set size, T<sub>max</sub> - number of templates • At most O(N) iterations • Each iteration is O(K<sub>L</sub> T<sub>max</sub> + K<sub>L</sub><sup>2</sup>)

# Summary

Given a collection, we jointly:

- Cluster models
- Learn a part-based deformable model
- Compute consistent segmentations
- Compute correspondences

Our algorithm is:

- Linear in size of collection
- Out-of-core
- Performs favorably on benchmark datasets

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#### Structure

Correspondences

Parts

Variations

Grouping





















Correspondences

Parts

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Grouping

Symmetry

#### What is missing?

#### 1. Define structure intrinsically:

- robust to articulation
- strong deformations

#### 2. Define structure hierarchically:

- more efficient
- can handle more complex objects or scenes



**Google Streetview** 



input single-view scan

**Microsoft Kinect** 









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# Thank you!

## **ADDITIONAL SLIDES**

## **Previous Work**



# **Previous Work**

## **3D repositories**

#### Structure

**Correspondences** 



#### Variations

Grouping



(c) Sidi et al. SIGGRAPH Asia'11, Huang et al. SIGGRAPH Asia'11
# **Previous Work**



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### Structure

Correspondences

Parts

#### Variations





(c) Kalogerakis et al., SIGGRAPH'12

# **Previous Work**



### Structure

Correspondences

Parts

#### Variations





Gears



Screws

(c) Hou et al., CAD'05

### **Recap + References**

